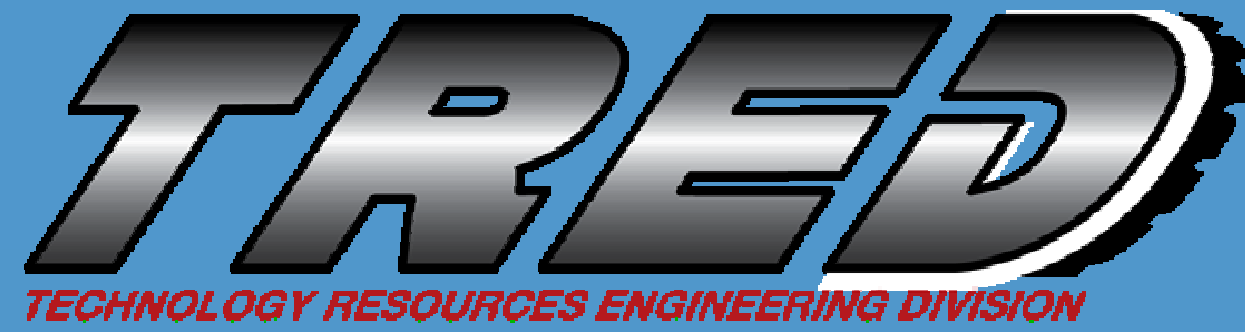


# Finite Element Analysis of (L)H<sub>2</sub> Cryogenic Capable Pressure Vessel Designs

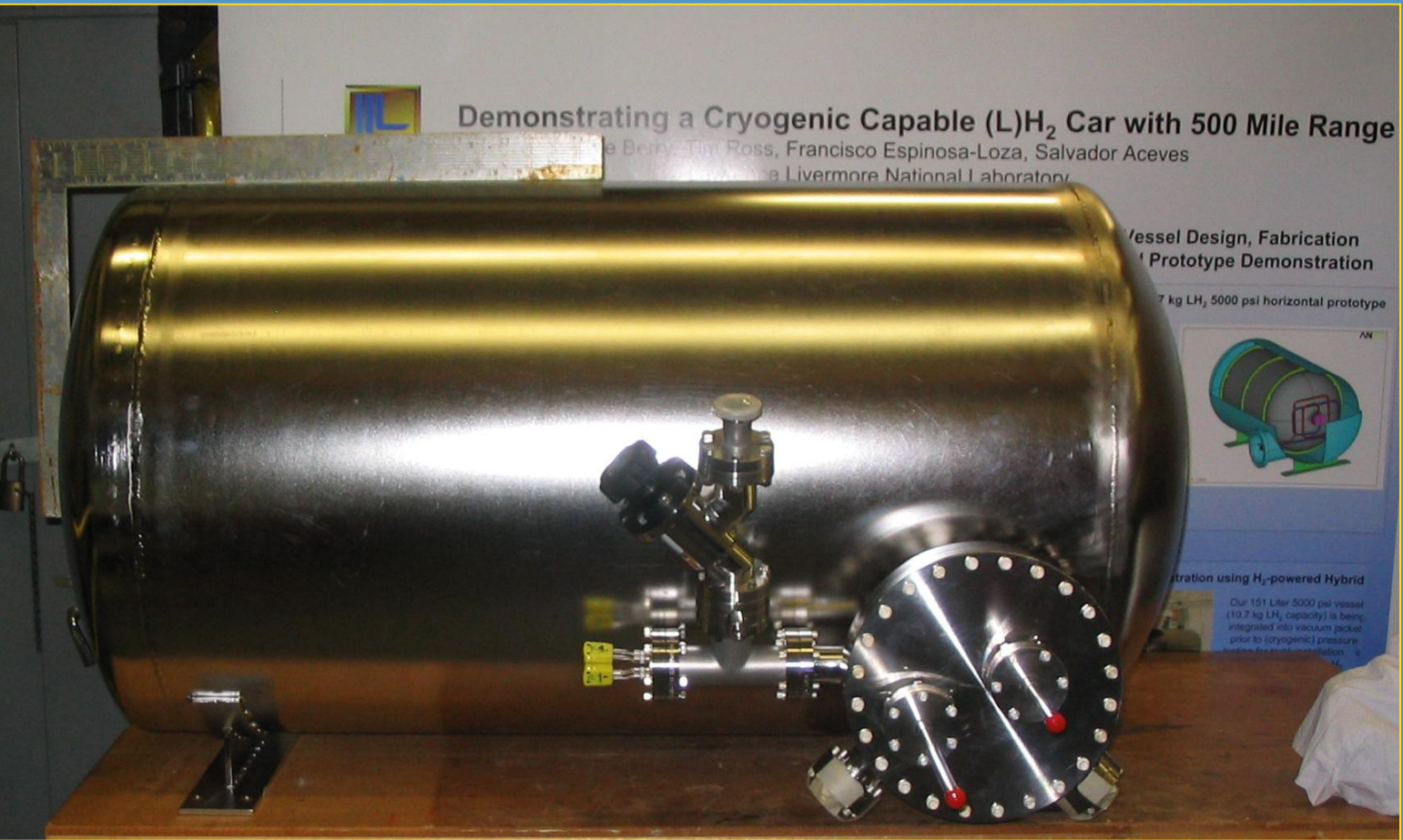


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## Introduction:

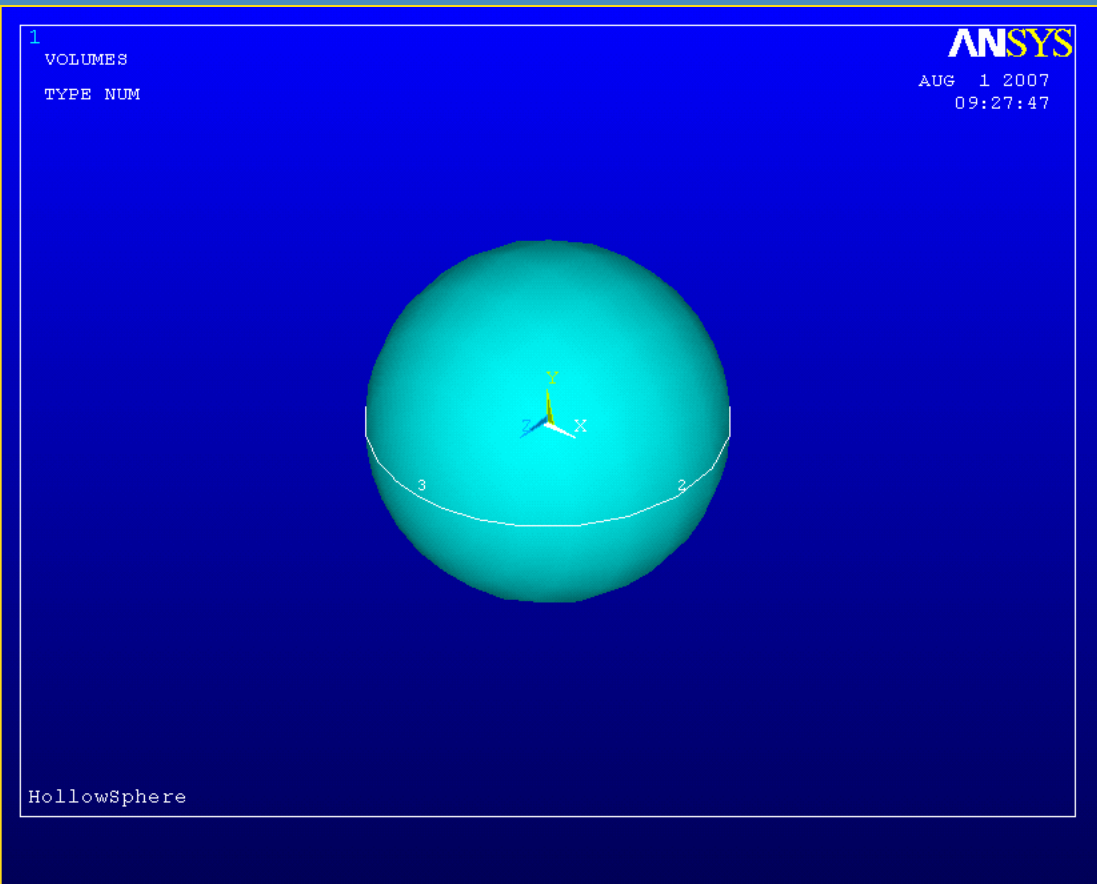


1. Cryogenic Capable Pressure Vessel

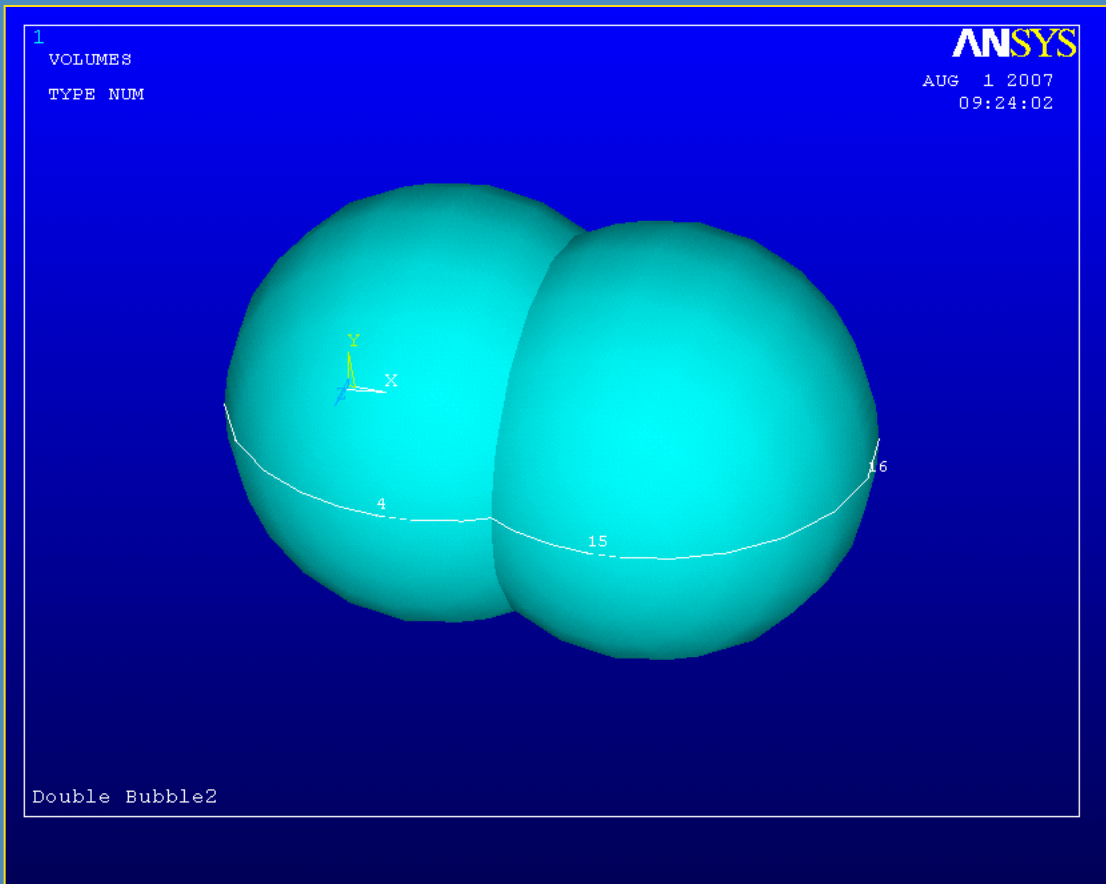
2. Hydrogen powered Toyota Prius

- There are four technologies suitable for vehicular hydrogen storage: compressed gas, metal hydride materials, carbon-based materials, and cryogenic liquid
- Each technology has a weakness: weight, volume storage efficiency, compression or liquefaction demand, or boiling loss
- LLNL's research efforts involves the usage of a cryogenic capable pressure vessel (CCPV)
- CCPV Advantages: long range, compact, eliminates LH<sub>2</sub> evaporation, flexible refueling

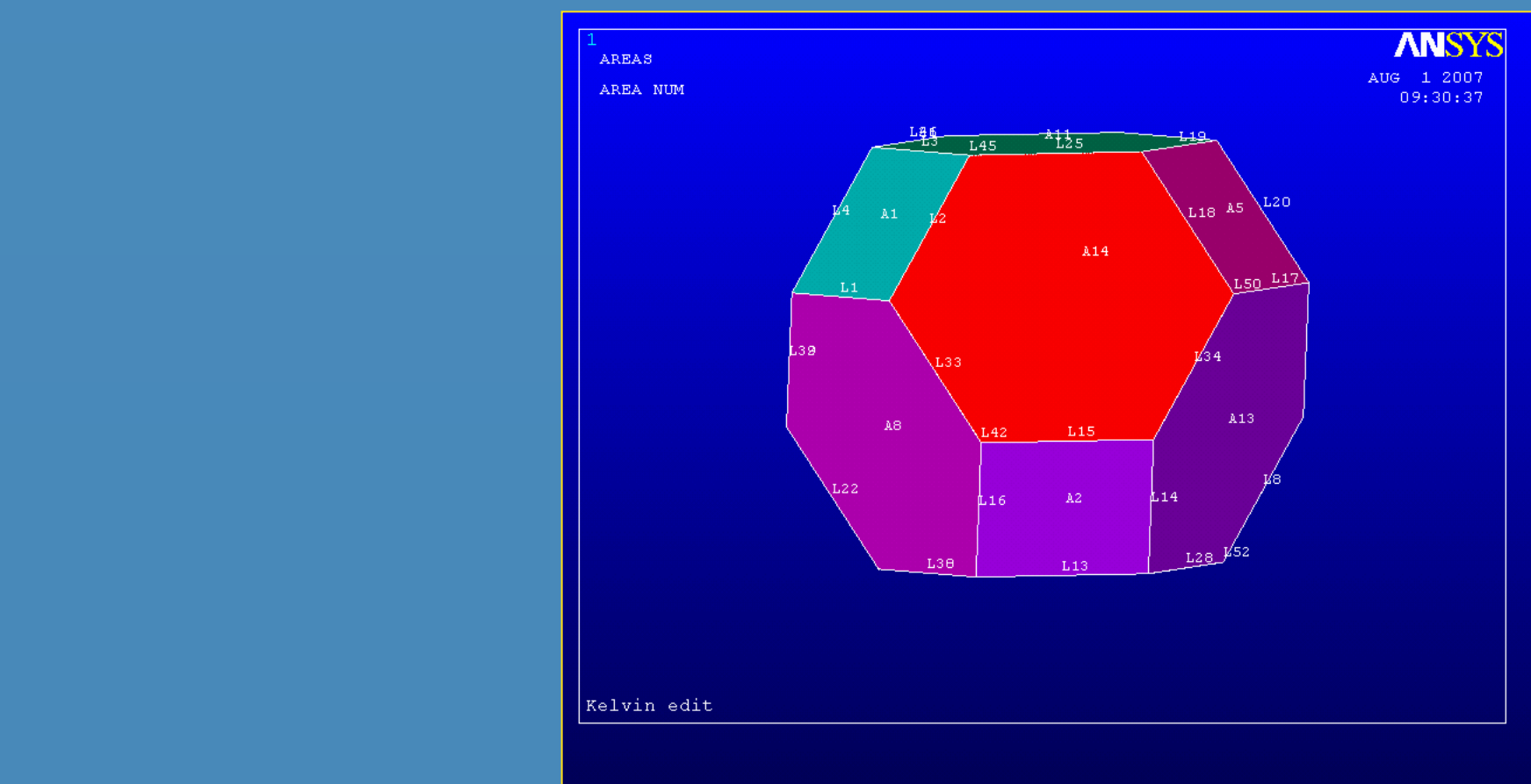
## Pressure Vessel Designs:



Sphere



Double Bubble



Kelvin Cell

3. Cryogenic Capable Pressure Vessel Designs

## Methodology:

- Finite element model of each design was created using Aluminum 6061 and subjected to various internal pressures
- Each model was analyzed with and without an outer carbon fiber/epoxy composite laminate layer
- A program was created to generated the elastic properties of the carbon fiber/epoxy composite laminate
- The model calculates the properties using three different micromechanics models: Rule of mixtures, Concentric cylinder, and Halpin-Tsai

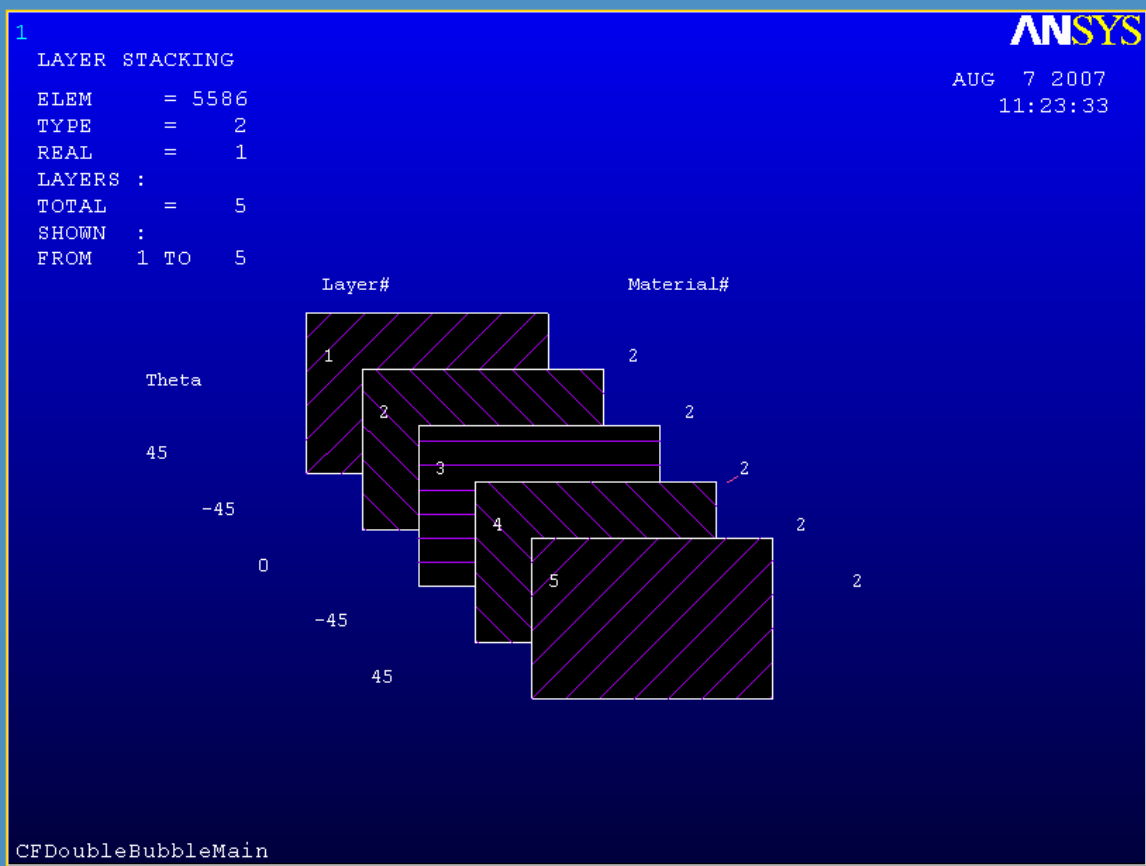
## Elastic Properties Model:

T300/BSL914C composite laminate stiffness matrix

140.6233	4.6844	4.6844	0	0	0
4.6844	12.5003	4.2297	0	0	0
4.6844	4.2297	12.5003	0	0	0
0	0	0	5.5000	0	0
0	0	0	0	4.1353	0
0	0	0	0	0	5.5000

T300/BSL914C composite laminate compliance matrix

0.0072	-0.0020	-0.0020	0	0	0
-0.0020	0.0909	-0.0300	0	0	0
-0.0020	-0.0300	0.0909	0	0	0
0	0	0	0.1818	0	0
0	0	0	0	0.2418	0
0	0	0	0	0	0.1818



4. Carbon Fiber Layup

### Rule of Mixtures Model

$$\begin{aligned} E_{c11} &= E_{f11}V_f + E_{e11}V_e \\ N_{Uc12} &= N_{Uf12}V_f + N_{Ue12}V_e \\ E_{c22} &= 1/((V_f/E_{f22}) + (V_e/E_{e22})) \\ G_{c12} &= 1/((V_f/G_{e12}) + (V_e/G_{e12})) \end{aligned}$$

### Concentric Cylinder Model

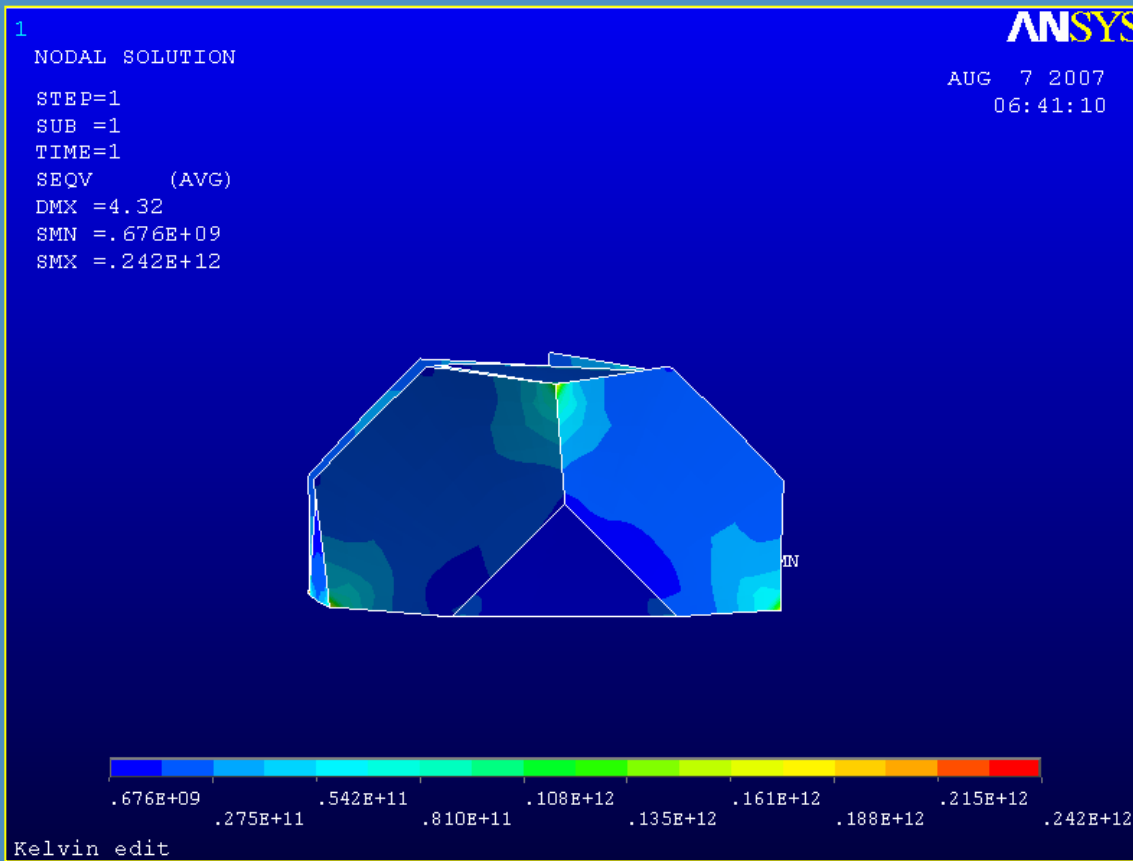
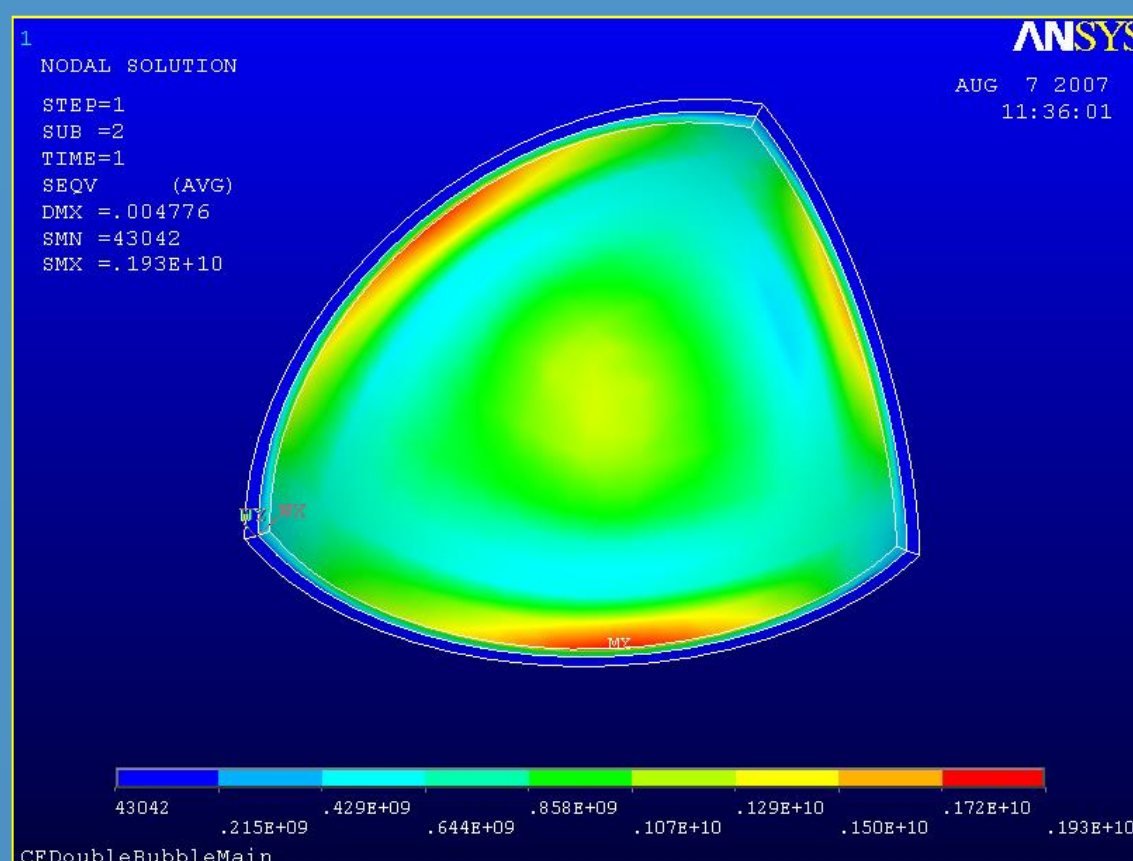
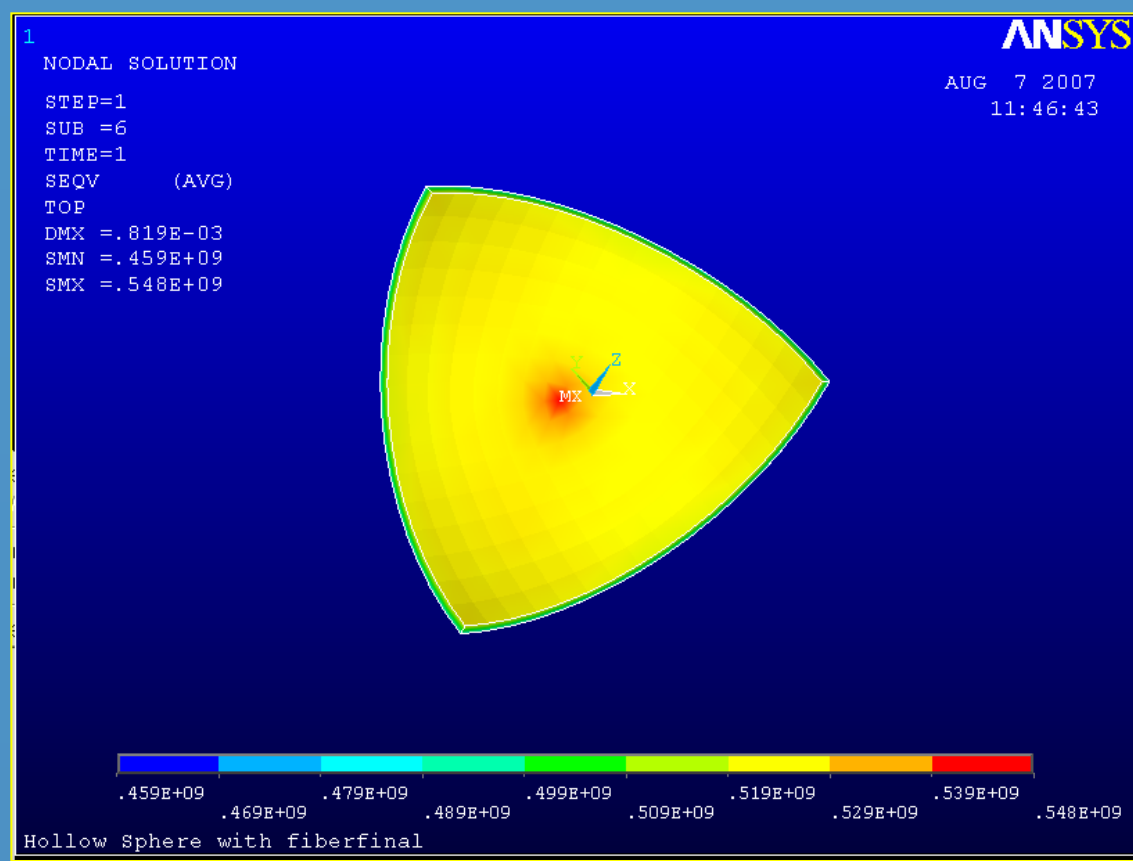
$$\begin{aligned} E_{c11} &= E_{f11}V_f + E_{e11}V_e + TT1 \\ N_{Uc12} &= N_{Uf12}V_f + N_{Ue12}V_e + TT2 \\ G_{c12} &= G_{e12} * (G_{f12} * (1 + V_f) + G_{e12} * (1 - V_f)) / ((G_{e12} * (1 - V_f)) + G_{e12} * (1 + V_f)) \\ G_{c23} &= G_{e23} * (1 + (1 + B1) * V_f / (P * V_f * (1 + 3 * (B1^2) * (V_e^2) / (A * (V_f^3) + 1)))) \\ E_{c22} &= 4 / (1 / G_{c23} + 1 / K_{c23} + 4 * (N_{Uc12}^2) / E_{c11}) \\ N_{Uc23} &= E_{c22} / (2 * G_{c23}) - 1 \end{aligned}$$

### Halpin-Tsai Model

$$\begin{aligned} E_{c11} &= E_{f11}V_f + E_{e11}V_e \\ N_{Uc12} &= N_{Uf12}V_f + N_{Ue12}V_e \\ G_{c12} &= G_{e12} * (1 + EPS\_G12 * ETA\_G12 * V_f) / (1 - ETA\_G12 * V_f) \\ E_{c22} &= E_{e22} * (1 + EPS\_E22 * ETA\_E22 * V_f) / (1 - ETA\_E22 * V_f) \\ G_{c23} &= G_{e23} * (1 + EPS\_G23 * ETA\_G23 * V_f) / (1 - ETA\_G23 * V_f) \end{aligned}$$

## Results:

- Due to the symmetry of the pressure vessel designs, full models of the designs were not required to properly analyze each design.
- The spherical design experienced the least stress of all the designs with or without carbon fiber
- The Kelvin Cell design experienced the most stress and displacement at 5000 psi
- The usage of carbon fiber on the designs reduced the stress experienced by each pressure vessel.



5. Cryogenic Capable Pressure Vessel Design Results with carbon fiber

## Discussion:

- The kelvin cell design has excellent packing characteristics, but it fails at high pressures
- The usage of a different material such as stainless steel 304 could increase the kelvin cell design resistance to failure
- The double bubble design uses the least area to enclose two equal volumes
- At 5000 psi, the carbon fiber wrapped spherical vessel design's von mises stress was 28.394% less than the double bubble
- Given the stress experienced by the spherical design, it is feasible to create a modular cubic cryogenic capable pressure with a spherical inner vessel and a cubic vacuum outer jacket.



6. Cubic Cryogenic Capable Pressure Vessel